9/14/2021

Maths Calculation Policy.

Britannia Community Primary School

Written by – N.Longstaff/D. Toddington

Date of agreement –September 2021

Maths Calculation Policy

This calculations policy supports the No Problem Singapore Maths scheme used throughout the school.

Progression within in each area of calculation is in line with the programme of study in the 2014 National Curriculum.

This calculation policy should be used to support children to develop a deep understanding of number and calculation. This policy has been designed to teach children through the use of concrete, pictorial and abstract methods/representations.

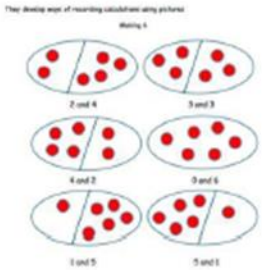
Concrete representation - a pupil is first introduced to an idea or a skill by acting it out with real objects. This is a 'hands on' component using real objects and it is the foundation for conceptual understanding.

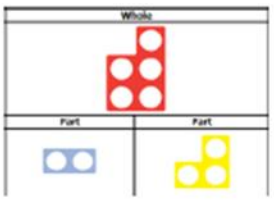
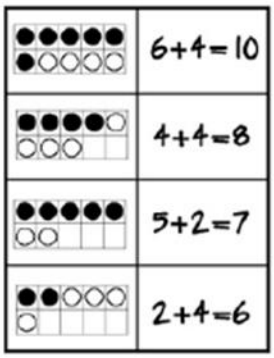
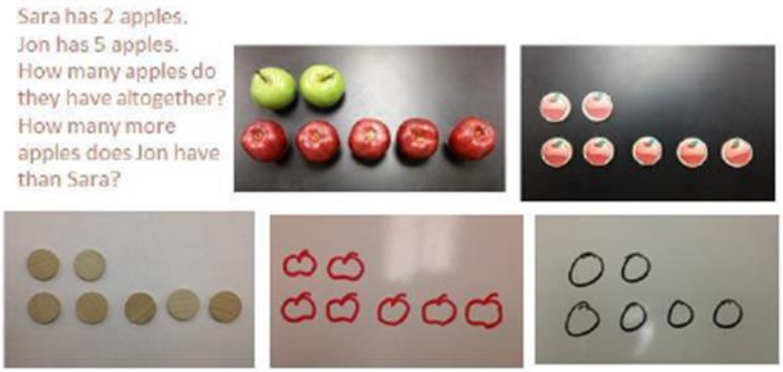
Pictorial representation - a pupil has sufficiently understood the hands-on experiences performed and can now relate them to representations, such as a diagram or picture of the problem.

Abstract representation - a pupil is now capable of representing problems by using mathematical notation, for example: $12 \div 2 = 6$.

It is important that conceptual understanding, supported by the use of representation, is secure for all procedures. Reinforcement is achieved by going back and forth between these representations.

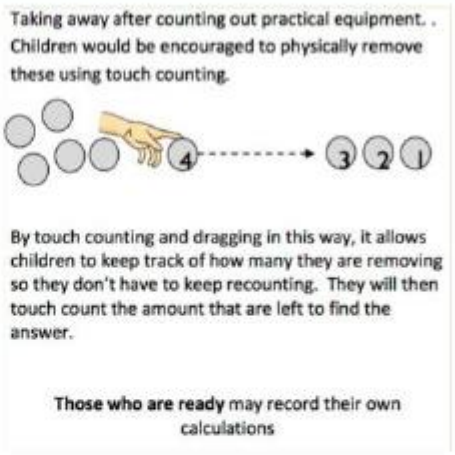
Calculation Policy
Britannia CP School
Reception

<table>
<tr><th colspan="2">Addition</th></tr>
<tr><td>Explore part part whole relationship - Combining two parts to make a whole</td><td> 

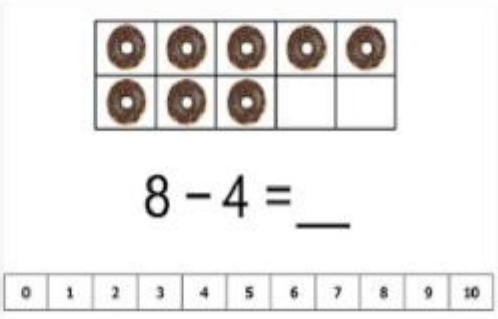


</td></tr>
<tr><td>Using the ten frame/ egg boxes to support addition of single digits - counting all/combining two groups</td><td> 
</td></tr>
<tr><td>Solving problems using concrete and pictorial images</td><td> 
</td></tr>
</table>

Subtraction

Using concrete strategies for counting.

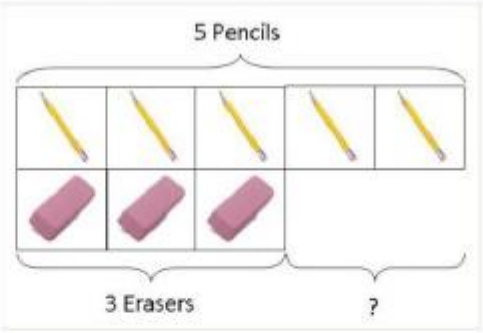


Using the ten frames to support subtraction by taking away.



Peter has 5 pencils and 3 erasers. How many more pencils than erasers does he have?

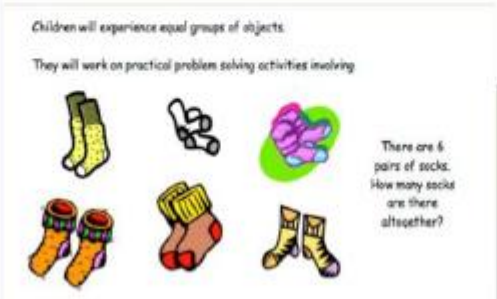
Solving problems using concrete and pictorial images.

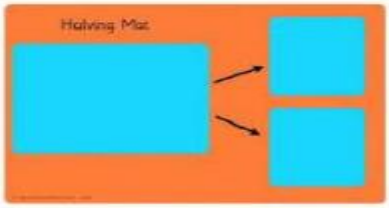


Multiplication

Experiencing equal groups of objects.

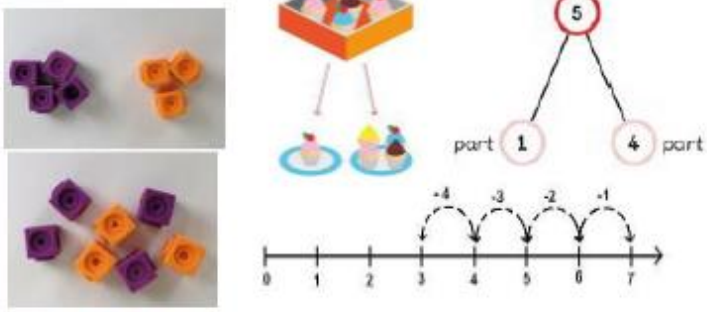
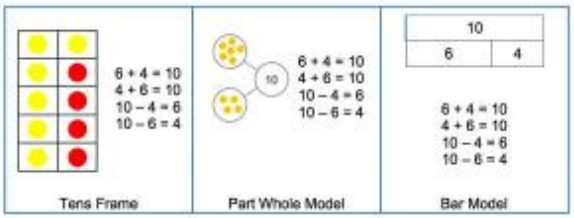
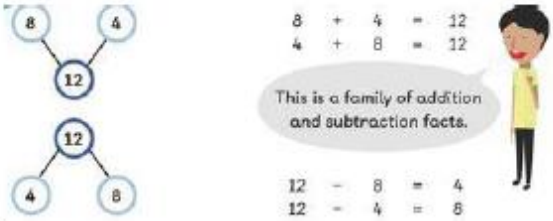
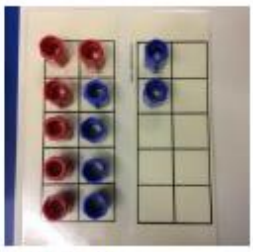
They will think about doubling when solving practical problems.

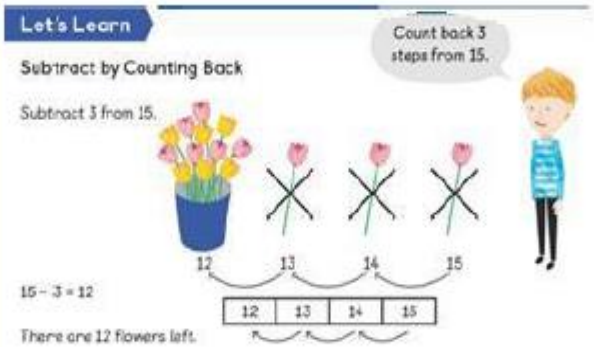
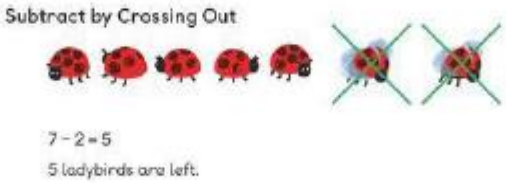
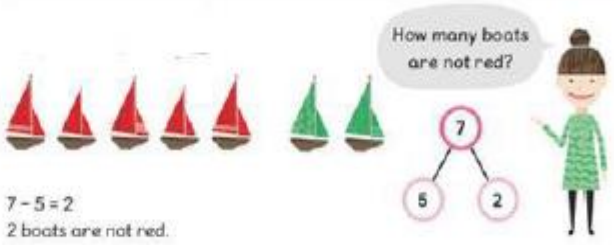


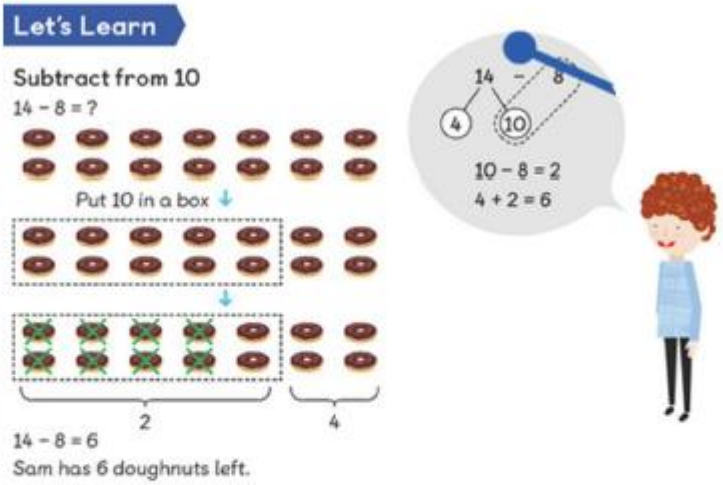
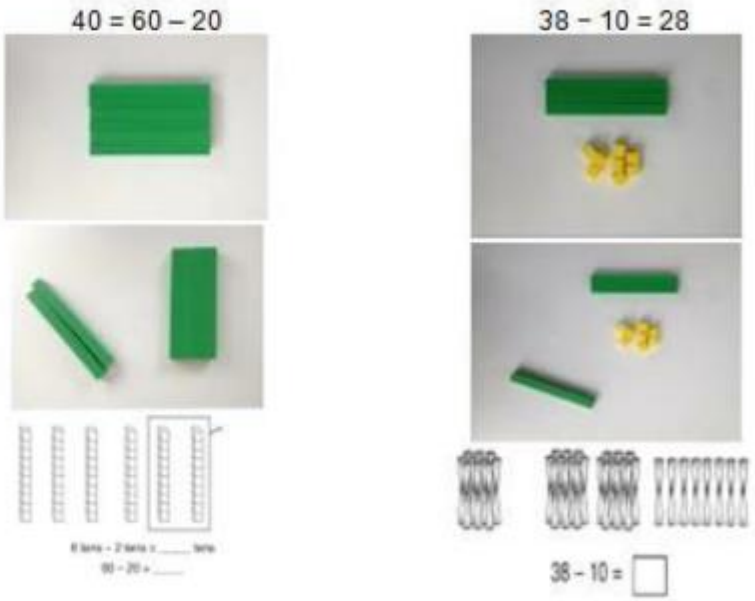
Division	
Sharing practical objects. Hearing and being exposed to language to describe half and seeing visual representatives.	 

Year 1

Addition

Combining two parts to make a whole: part-whole model. Joining two groups and then recounting all objects (lots of practice making 10 and numbers to 10 e.g. 6 + 4 = 10 or 3 + 5 = 8)	3 + 4 = 7 
Number Bonds Learn number bonds to 20 and demonstrate related facts. Addition and subtraction taught alongside each other as pupils need to see the relationship between the facts.	 
Add and subtract one digit numbers and two digit numbers to 20, including zero	8+1=9 
Bridging 10: use ten frames, Singapore bars, egg boxes and number lines to practice. Children should start with the larger number and add the smaller number seeing what makes ten.	 6 + 6 = 12  Make 9 in one and 3 in the other. Take one from the 3 to make the 9 into a ten....10+2 = 12

Subtraction	
Taking away should begin with physical objects: counters, cubes, Dienes etc	 6 -3=3
Subtraction by counting back	
Subtracting a single digit number from a single digit number and a single digit from a two digit by crossing out pictures	
Subtracting using the part part whole model (include problem solving with missing digits). ? - 5 = 2	

Subtraction by subtracting from 10 *Children subtract from 10 and not from ones*	14 – 8 = ? 
When subtracting using Dienes children should be taught to regroup (rename) a ten rod for 10 ones and then subtract from those ones	 20 – 4 = 16
Subtracting multiples of 10 *Using the vocabulary of 1 ten, 2 tens etc alongside 10, 20, 30 Is very important here as pupils need to understand that it is a 10 not a 1 that is being taken away*	

BRITANNIA CP SCHOOL
BACUP

Multiplication

Counting in multiples of 2, 5 and 10 from zero

Children should count

the number of groups on their fingers as they are skip counting

4 groups of 2 = 8

4 x 2 = 8

2 × 4 = 8

When moving to pictorial/written calculations the vocabulary is important

This image represents two groups of 4 or 4 twice

Solving multiplication problems using repeated addition

How many apples are there altogether?

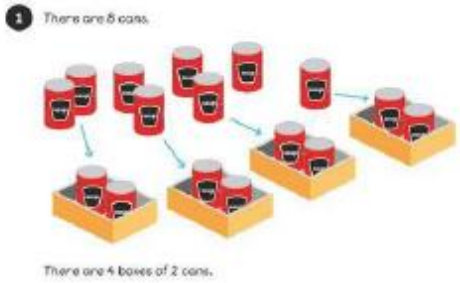
3 + 3 + 3 = 9

Division

Pupils should be taught to divide through working practically and the sharing should be shown below the whole to familiarize children with the concept of the whole.

The language of whole

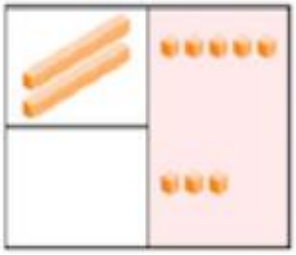
10 ÷ 2 = 5



Year 2

Addition

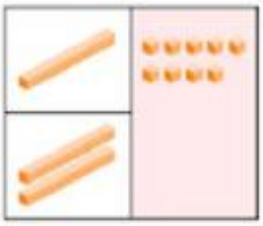
Using concrete objects and pictorial representations to add a 2 digit number with a 1 digit number.



	tens	ones
	2	5
+		3
		8

Using concrete objects and pictorial representations to add a 2 digit number and 10s number.

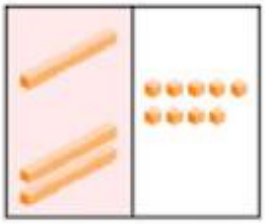
Step 1 Add the ones.



	tens	ones
	1	9
+	2	0
		9

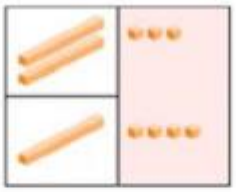
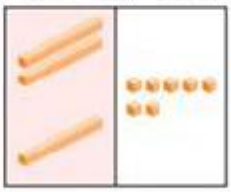
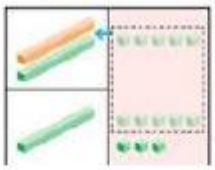
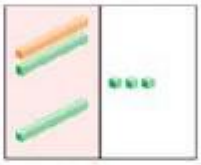
Step 2 Add the tens.

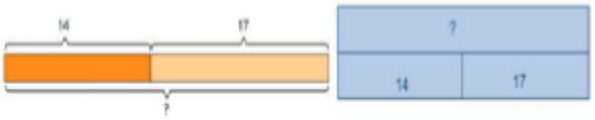
1 ten + 2 tens = 3 tens



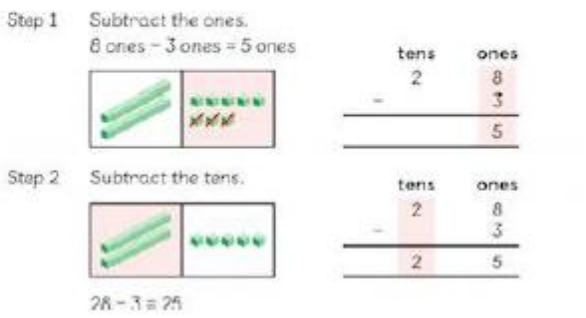
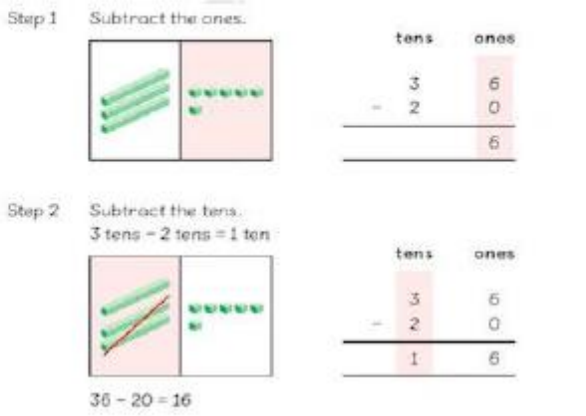
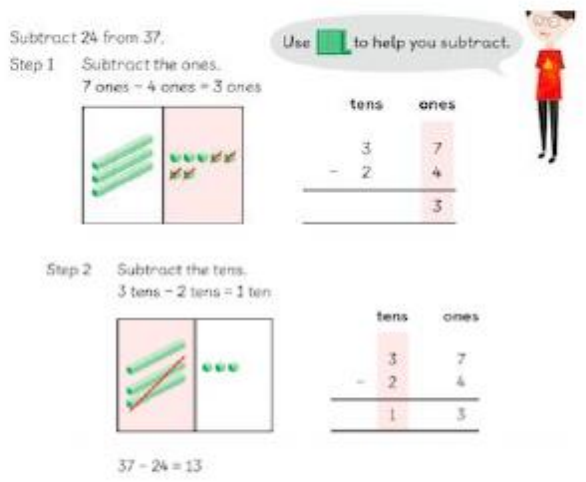
	tens	ones
	1	9
+	2	0
	3	9

19 + 20 = 39

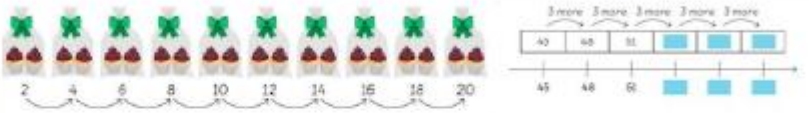
Using concrete objects and pictorial representations to add 2 2-digit numbers.	Step 1 Add the ones. 3 ones + 4 ones = 7 ones  tens ones 2 3 + 1 4 7 Step 2 Add the tens. 2 tens + 1 ten = 3 tens  tens ones 2 3 + 1 4 3 7 23 + 14 = 37 **Adding with renaming** Add 15 and 18. Use to help you add.  Step 1 Add the ones. 5 ones + 8 ones = 13 ones Regroup the ones. 13 ones = 1 ten and 3 ones  tens ones 1 5 + 1 8 1 3 Step 2 Add the tens. 1 ten + 1 ten + 1 ten = 3 tens  tens ones 1 5 + 1 8 1 3 + 2 0 3 3 15 + 18 = 33
Using concrete objects and pictorial representations to add 3 single digit numbers.	7+3+2 = leads to 10 + 2 =  

Using the bar to find missing digits. *It is important for children to use the bar in this way to encourage the use of it to aid with problem solving.*	Helen has 14 bread-sticks. Her friend has 17. How many do they have altogether? 

Subtraction

Using concrete objects and pictorial representations to subtract a 1 digit number from 2 digit number.	
Using concrete objects and pictorial representations to subtract a 10s number from 2 digit number.	
Using concrete objects and pictorial representations to subtract a 2 digit number from 2 digit number.	

Recognise and use the inverse relationship between addition and subtraction	?			76		Use this to check calculations and solve missing number problems.
	23	53		23	?	

<table>
<tr><th colspan="2">Multiplication</th></tr>
<tr><td>Skip counting in multiples
of 2, 3, 5, 10 from 0</td><td> 
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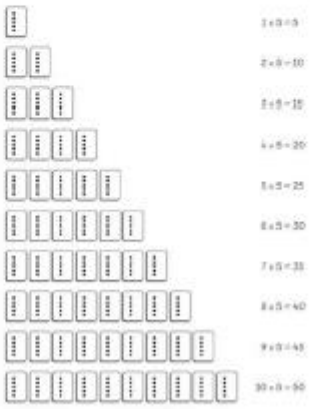
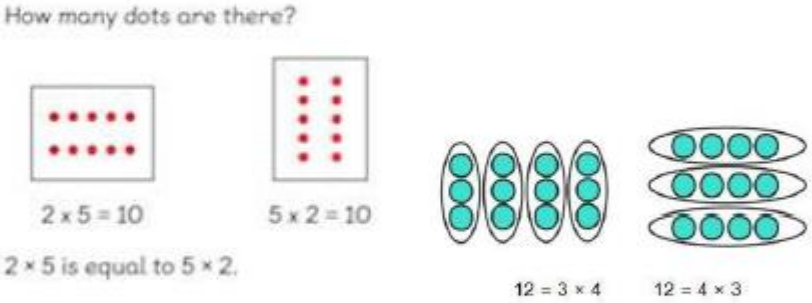
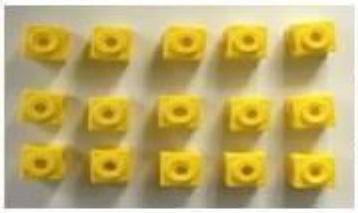
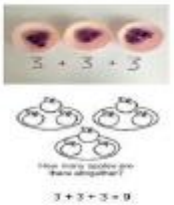
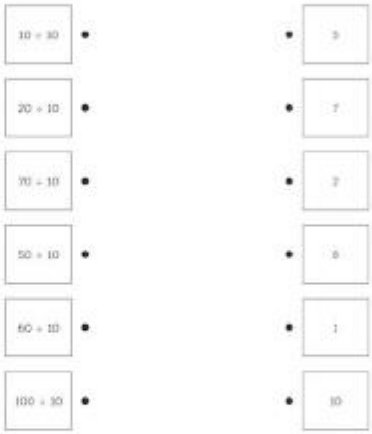
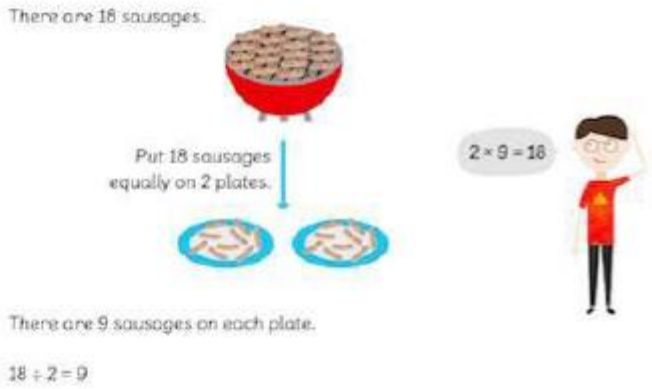
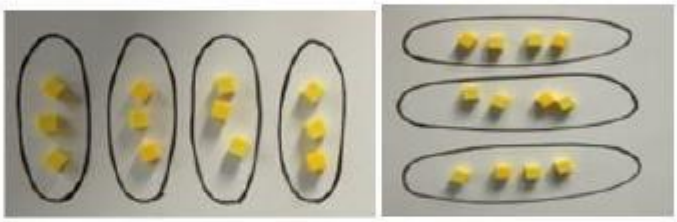
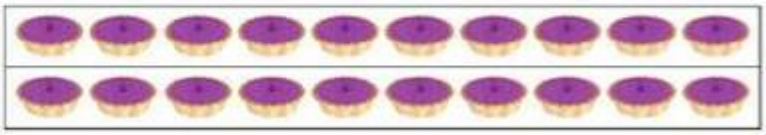
<tr><td>Recall and use multiplication facts for the multiplication tables 2, 5 and 10.</td><td>  </td></tr>
<tr><td>Use multiplication (x) and equal (=) sign when writing out times tables.</td><td>  </td></tr>
<tr><td>Understanding Multiplication is commutative

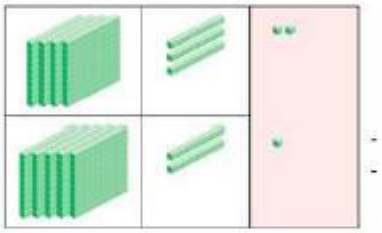
Pupils should understand that an array can represent different equations and that, as multiplication is commutative, the order of the multiplication does not affect the answer.</td><td> 
</td></tr>
</table>

Solve multiplication problems in context using arrays and repeated addition	 3 x 5 = ☐ 5 x 3 = ☐ 

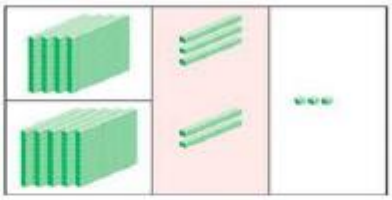
<table>
<tr><th colspan="2">Division</th></tr>
<tr><td>Recall and use division facts for the multiplication tables 2, 5 and 10.</td><td>  </td></tr>
<tr><td>Solve division problems in context using concrete objects by sharing</td><td> 
</td></tr>
<tr><td>Solve division problems in context using arrays</td><td>  </td></tr>
<tr><td>Solve division as grouping.</td><td> 
</td></tr>
</table>

	 Put into groups of 5. There are ☐ groups.
use the inverse This should be taught alongside both multiplication and division.	Make a family of multiplication and division facts.  2 x 10 = 20 ——— 20 ÷ 10 = ☐ 10 x 2 = 20 ——— 20 ÷ 2 = ☐

Year 3

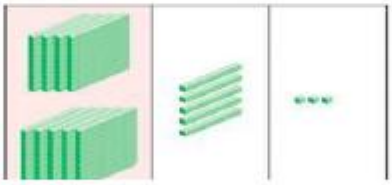
Addition	
Add two three digit numbers. *Children need to use equipment first to support their understanding of place value.* *Starting without renaming and gradually moving towards renaming.*	432 + 521 = Step 1 Add the ones. 2 ones + 1 one = 3 ones  h t o 4 3 2 + 5 2 1 3

Step 2 Add the tens.
3 tens + 2 tens = 5 tens



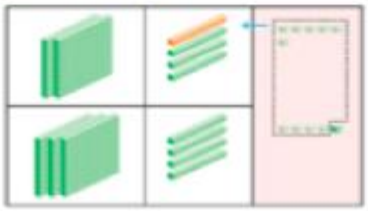
	h	t	o
	4	3	2
+	5	2	1
		5	3

Step 3 Add the hundreds.
4 hundreds + 5 hundreds = 9 hundreds



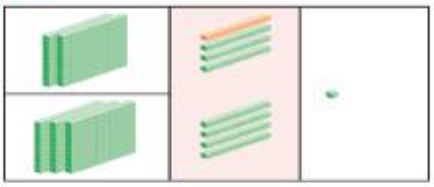
	h	t	o
	4	3	2
+	5	2	1
	9	5	3

236 + 345 =



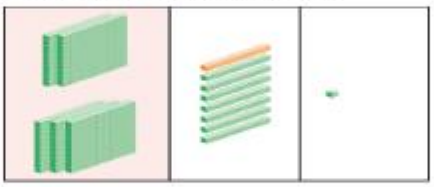
	h	t	o
	2	3	6
+	3	4	5
			1

Step 2 Add the tens.
1 ten + 3 tens + 4 tens = 8 tens



	h	t	o
	2	3	6
+	3	4	5
		8	1

Step 3 Add the hundreds.
2 hundreds + 3 hundreds = 5 hundreds

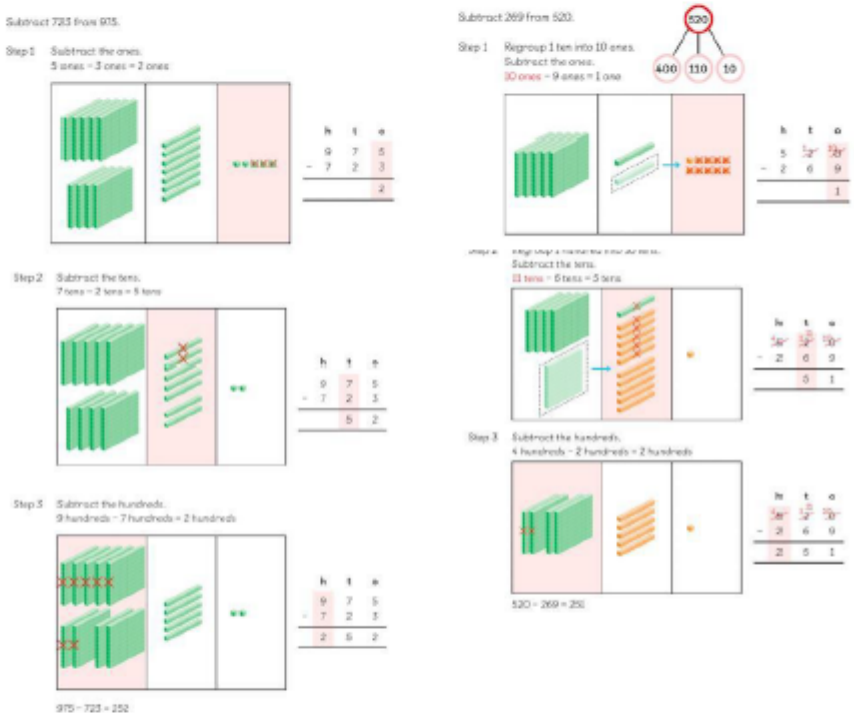


	h	t	o
	2	3	6
+	3	4	5
	5	8	1

236 + 345 = 581

Bar modeling It is important for children to use the bar in this way to encourage the use of it to aid with problem solving.	**Bar Model to support understanding of problem solving:** A man sold 230 balloons at a carnival in the morning. He sold another 86 balloons in the evening . How many balloons did he sell in all? 

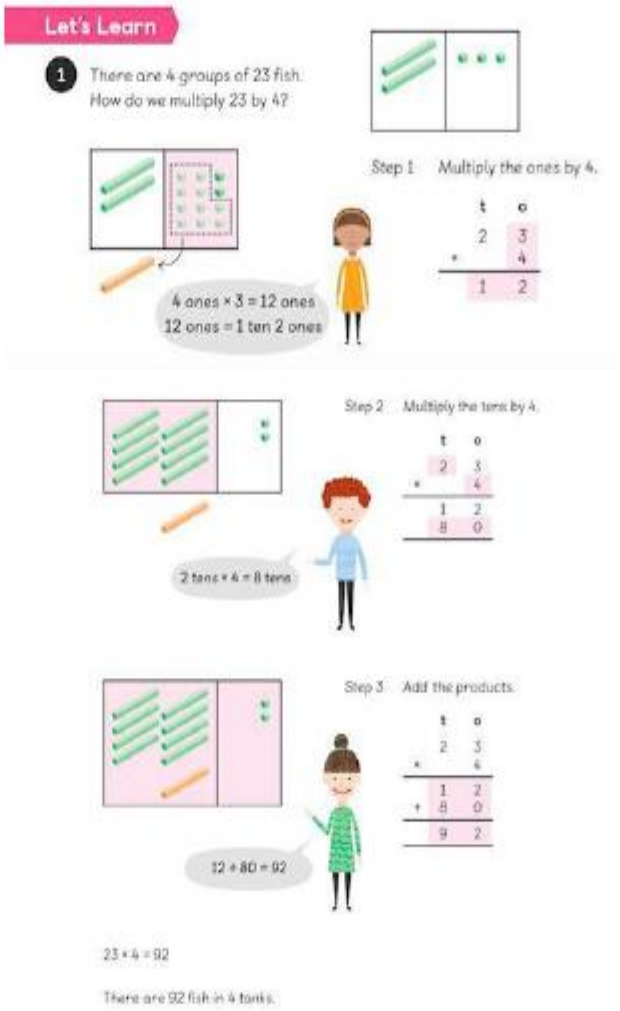
Subtraction

Subtract up to 3 digits from 3 digits. *Very important for children to use dienes equipment along with a place value chart to support.* Only when secure with the method should exchanging be introduced.	
Using the bar to find missing number. *It is important for children to use the bar in this way to encourage the use of it to aid with problem solving.*	315 – 185 = ? 185 + ? = 315 185 + 315 = ? ? – 185 = 315

Multiplication

Children should be able to recall the 2, 5, 10, 3, 4 and 8 times tables.

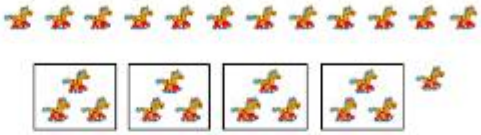
Multiply a two digit number by a one digit.

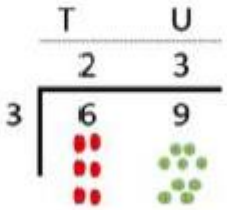


Using the bar to solve multiplication problems.

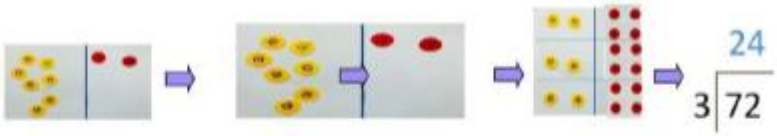
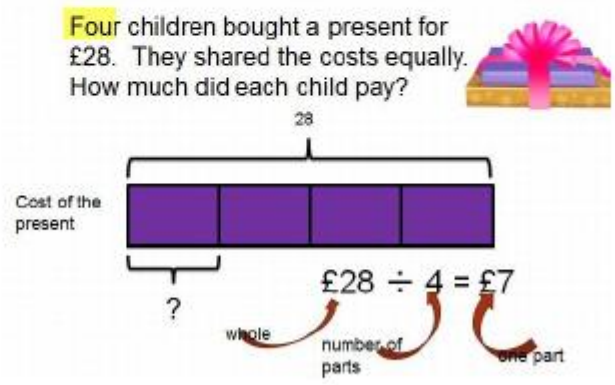
4 children go to the cinema. They each pay £15. How much do they spend altogether?

Whole unknown

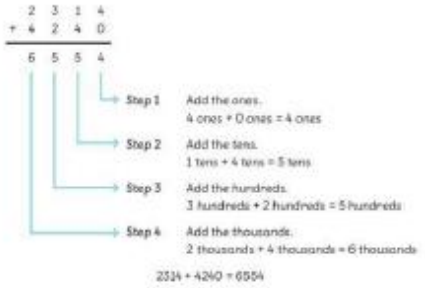
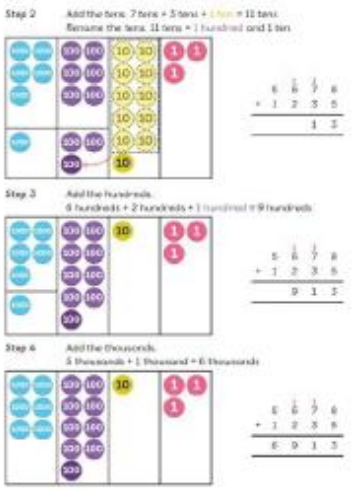
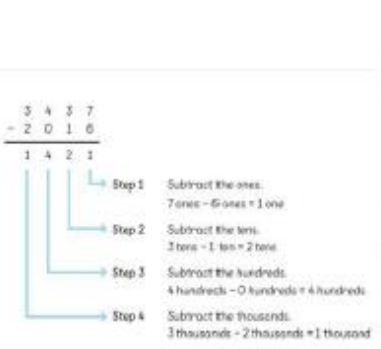
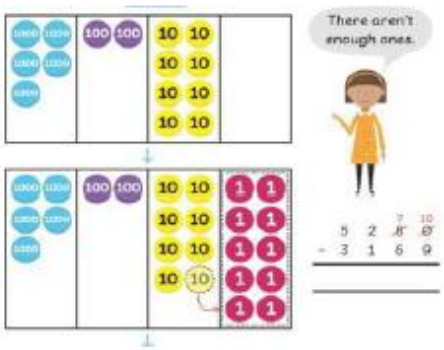
<table>
<tr><th colspan="2">Division</th></tr>
<tr><td>Dividing by grouping understanding the concept of remainders.</td><td>Start with using the real objects-or objects that represent the calculation.
 
13 ÷ 4 = 3 Remainder 1</td></tr>
<tr><td>Dividing using short division.

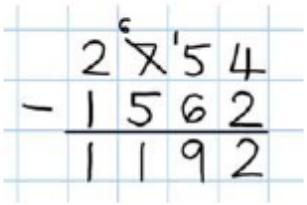
Once children are secure with division as grouping and demonstrate this using number lines, arrays etc., short division for larger 2-digit numbers should be introduced, initially with carefully selected examples requiring no Calculating of remainders at all. Start by introducing the layout of short division by comparing it to an array.</td><td> 

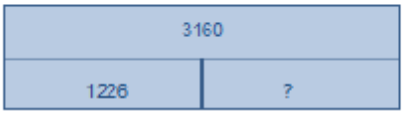
Remind children of correct place value, that 69 is equal to 60 and 9, but in short division, pose:
· How many 3's in 6? = 2, and record it above the 6 tens.
· How many 3's in 9? = 3, and record it above the 9 ones.

Once children demonstrate a full understanding of remainders, and also the short division method taught, they can be taught how to use the method when remainders occur within the calculation (e.g. 72÷3), and be taught to 'carry' the remainder onto the next digit.
 
</td></tr>
<tr><td>Using the bar to aid the solving of division problems.</td><td> 
</td></tr>
</table>

Year 4

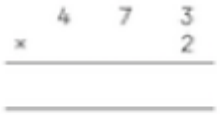
Addition	
Adding numbers with up to 4 digits. *Again this should start with the children using dienes to support them with lots of discussion about the value of each digit.*	 
Using the bar to find missing digits. *It is important for children to use the bar in this way to encourage the use of it to aid with problem solving.*	This is not a form of getting the correct answer but helping to guide children to the correct operation. Alison jogs 6,860 metres and Calvin jogs 5,470 metres. How far do they jog altogether? 
Subtraction	
Subtract with numbers up to four digits including exchanging when children are secure. *Again children need to use dienes to support their learning.*	 

<table>
<tr><td></td><td> 
</td></tr>
<tr><td>Using the bar to find missing digits.

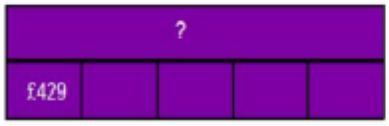
It is important for children to use the bar in this way to encourage the use of it to aid with problem solving.</td><td>There are 3,160 books in a shop. 1,226 are in English and the rest are in French. How many French books are there?
 
</td></tr>
<tr><td colspan="2">Multiplication</td></tr>
<tr><td>Children to know all times tables to 12 x 12.

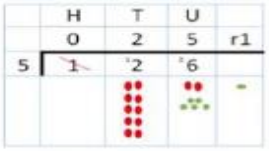
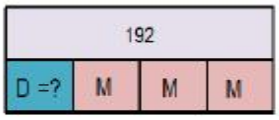
Ladder method to be used with children multiplying both two and three digits by a one digit number.</td><td>3 1 4
× 3
1 2 (3 x 4)
3 0 (3 x 10)
+ 9 0 0 (3 x 300)
9 4 2

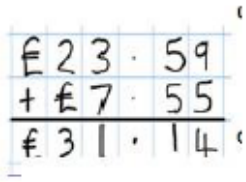
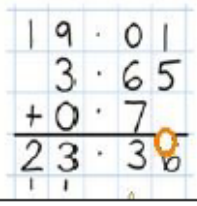
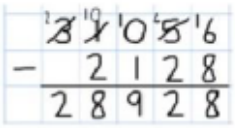
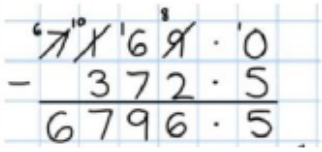
 
</td></tr>
<tr><td>Multiplying using the bar.</td><td>A computer costs 5 times as much as a television. The television costs £429.

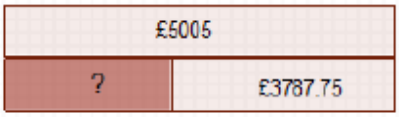
How much does the computer cost?

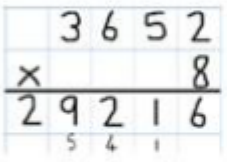
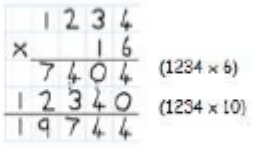
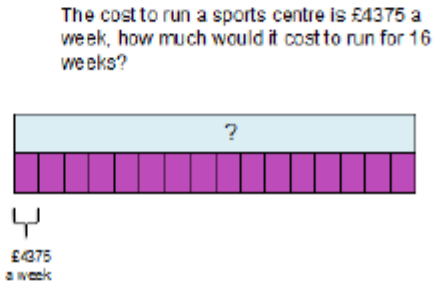
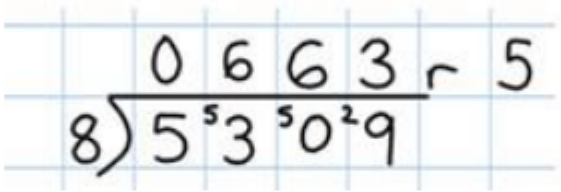
Cost of the computer
 
</td></tr>
</table>

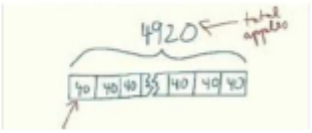
Division	
Dividing up to three digit numbers by a one digit number using short division. Only when the children are secure with dividing a two-digit number should they move onto a 3-digit number.	 
Dividing using the bar.	Desmond and Melissa collect cards. They have 192 cards in all. Melissa has three times as many cards as Desmond. How many cards does Desmond have? 

Year 5

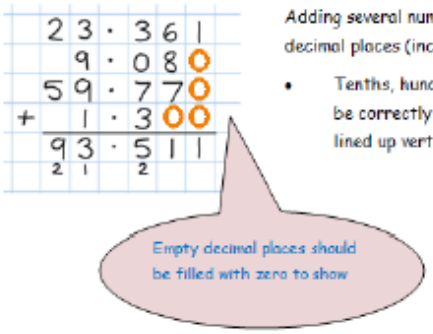
Addition	
Adding numbers with more than 4 digits including decimals *Using place value charts are key to this as well as place value counters to help with the decimals*	  
Using the bar to find missing digits. *It is important for children to use the bar in this way to encourage the use of it to aid with problem solving.*	This is not a form of getting the correct answer but helping to guide children to the correct operation. MacDonalds sold £9957.68 worth of hamburgers and £1238.5 worth of chicken nuggets. How much money did they take altogether? 
Subtraction	
Subtract with at least four digit numbers including two decimal places. *Include money, measures and decimals ensuring that children do this practically before the abstract.*	Subtract with decimal values, including mixtures of integers and decimals, aligning the decimal point.  

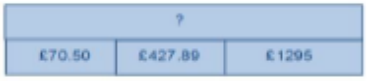
Using the bar to find missing digits. *It is important for children to use the bar in this way to encourage the use of it to aid with problem solving.*	A whole to Lapland costs £5005 for a family of four, the Smith's have only saved £3787.75, how much money do they still need to find? 
Multiplication	
Multiplying up to four digit numbers by two digits using long multiplication. *Children need to be taught to approximate first, e.g. for **72 x 38**, **they will use rounding:** 72 x 38 is approximately 70 x 40 = **2800**, and use the approximation to check the*	56 X 27 ——— 392 (56x7) 1120 (56x20) ——— 1512 Explain that first we are multiplying the top number by 7 starting with the units. (any carrying needs to be done underneath the numbers).

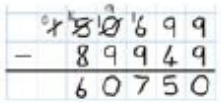
reasonableness of their answer.	· Now explain that we need to put a 0 underneath—explain that this is because we are multiplying the number by 20.. (2 tens) which is the same as multiplying 10 and 2. · Now add the 2 numbers together to give you the answer. · This will need lots of modeling to show the children.   (1234 × 6) (1234 × 10)
Using the bar to support multiplication.	
Division	
Diving with up to four digit numbers by one digit including numbers where remainders are left.	 **Short division with remainders:** Now that pupils are introduced to examples that give rise to remainder answers, division needs to have a real life problem solving context, where **pupils consider the meaning of the remainder and <u>how</u> to express it,** ie. as a fraction, a decimal, or as a rounded number or value , depending upon the context of the problem.

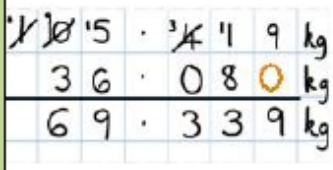
Using the bar to support division problems.	**Bar Model to support understanding of problem solving:** Frank has 4920 apples. He needs to put them into baskets of 40. How many baskets does he need? 

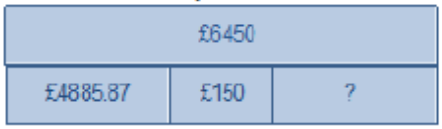
Year 6

<table>
<tr><th colspan="2">Addition</th></tr>
<tr><td>Adding several numbers with up to three decimal places.</td><td>


Adding several numbers with different numbers of decimal places (including money and measures):
• Tenths, hundredths and thousandths should be correctly aligned, with the decimal point lined up vertically including in the answer row.
</td></tr>
<tr><td>Adding using the bar.</td><td>
Jack went on holiday. His flight cost £70.50, the hotel £1295 and spending money £427.89. How much did Jack spend on his holiday?


</td></tr>
<tr><th colspan="2">Subtraction</th></tr>
<tr><td>Subtracting with increasingly large and more complex numbers and decimal values.</td><td>
Very important to use in a range of contexts- measures and money.


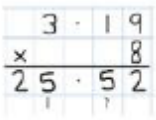


</td></tr>
<tr><td>Using the bar for subtraction.</td><td>
Chloe wants to buy a new car for £6450. She has £4885.87 in her savings account. Her Dad gives her £150 for her birthday. How much more money does she need to save?


</td></tr>
</table>

Multiplication

Short and long multiplication with up to two decimal places.

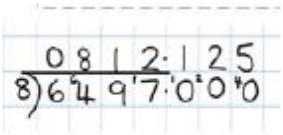


Using the bar to help with multiplication.

If 5 friends went on holiday and each paid £579.75 what was the total cost of the holiday?

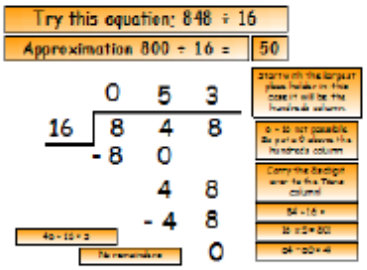
Division

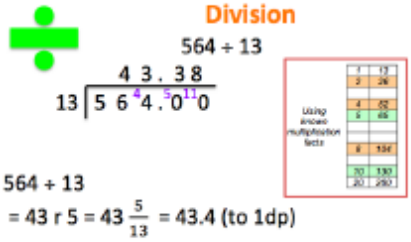
digits by both single digit and 2 digit numbers. (including decimal numbers and quantities)



Short division with remainders: Pupils should continue to use this method, but with numbers to at least 4 digits, and understand how to express remainders as fractions, decimals, whole number remainders, or rounded numbers. Real life problem solving contexts need to be the starting point, where pupils have to consider the most appropriate way to express the remainder.

Long division this is for when dividing by two digit numbers.





Using the bar to help divide.

Paul and David hire a car together at a cost of £297.50. Paul pays 6 times more than David. How much does David pay?